

**Class –T.Y.B.Sc**  
**Semester-VI**  
**Paper-IV –Number theory and its applications –II**

	<b>SAMPLE QUESTIONS</b>
1	The number of quadratic residue modulo 71 are (a) 30      (b) 35      (c) 40      (d) 45
2	$\left(\frac{2}{p}\right) = -\left(\frac{2}{p}\right)$ (a) $p \equiv 1 \pmod{4}$ (b) $p \equiv 3 \pmod{4}$ (c) $p \equiv 3 \pmod{5}$ (d) $p \equiv 1 \pmod{5}$
3	If $\left(\frac{a}{p}\right) = 1$ then $\left(\frac{p-a}{p}\right) = 1$ if (a) $p \equiv 1 \pmod{4}$ (b) $p \equiv 3 \pmod{4}$ (c) $p \equiv 3 \pmod{5}$ (d) $p \equiv 1 \pmod{5}$
4	$\left(\frac{71}{73}\right) =$ (a) $\left(\frac{2}{71}\right)$ (b) $\left(\frac{1}{71}\right)$ (c) $\left(\frac{3}{71}\right)$ (d) $\left(\frac{-1}{71}\right)$
5	$\left(\frac{7}{45}\right) =$ (a) $\left(\frac{7}{3}\right)$ (b) $\left(\frac{7}{9}\right)$ (c) $\left(\frac{2}{5}\right)$ (d) $\left(\frac{2}{7}\right)$
6	If a and b are two quadratic non residues modulo an odd prime p Then (a) ab is quadratic non residue modulo p (b) ab is quadratic residue modulo p (c) ab is quadratic non residue modulo any power of p (d) None of these
7	If p is an odd prime and a and b are relatively prime to p then $\left(\frac{a}{p}\right) \equiv r \pmod{p}$ Then, (a) $r = a^{\frac{p^2+1}{2}}$ (b) $r = a^{\frac{p^2-1}{2}}$ (c) $r = a^{\frac{p+1}{2}}$ (d) $r = a^{\frac{p-1}{2}}$
8	$\frac{61}{48}$ represents (a) [1,4,3,3,2]      (b) [1,4,1,3,2]      (c) [1,2,1,3,4]      (d) [1,3,1,2,4]

9	<p>Which of the following is a correct statement?</p> <p>(a) The convergents with odd subscripts form a strictly increasing sequence.</p> <p>(b) The convergents with even subscripts form a strictly decreasing sequence.</p> <p>(c) Every convergent with an even subscripts is greater than every convergent with an odd subscript.</p> <p>(d) A rational number can be written as a finite simple continued fraction</p>
10	<p>If <math>\gcd(a, b) = 1</math> and <math>\frac{a}{b} = [a_0, a_1, \dots, a_n]</math> where <math>n</math> is odd Then,</p> <p>(a) <math>x = aq_{n-1}</math> &amp; <math>y = -bP_{n-1}</math> gives a solution of <math>ax + by = c</math></p> <p>(b) <math>x = -aq_{n-1}</math> &amp; <math>y = bP_{n-1}</math> gives a solution of <math>ax + by = c</math></p> <p>(c) <math>x = -cq_{n-1}</math> &amp; <math>y = cP_{n-1}</math> gives a solution of <math>ax + by = c</math></p> <p>(d) <math>x = cq_{n-1}</math> &amp; <math>y = -cP_{n-1}</math> gives a solution of <math>ax + by = c</math></p>
11	<p>The congruence <math>x^2 \equiv 5 \pmod{227}</math> has</p> <p>(a) Only 1 solution</p> <p>(b) Two solutions</p> <p>(c) Three solutions</p> <p>(d) No solutions</p>
12	<p>For SCF <math>[0, 3, 2, 1, 1, 4]</math> convergents <math>C_2</math> and <math>C_3</math> is given by</p> <p>(a) <math>C_2 = 0, C_3 = 2</math></p> <p>(b) <math>C_2 = 3/10, C_3 = 2/7</math></p> <p>(c) <math>C_2 = 2/7, C_3 = 3/10</math></p> <p>(d) <math>C_2 = 10/3, C_3 = 7/2</math></p>
13	<p>If <math>C_k = \frac{p_k}{q_k}</math> is the <math>k^{th}</math> convergent of SICF <math>[a_0, a_1, a_2, \dots, \dots, \dots]</math> then for <math>k \geq 2</math> then,</p> <p>(a) <math>q_k &gt; (2)^{\frac{k-1}{2}}</math></p> <p>(b) <math>q_k \leq (2)^{\frac{k-1}{2}}</math></p> <p>(c) <math>q_k \geq (2)^{\frac{k-1}{2}}</math></p> <p>(d) <math>q_k &lt; (2)^{\frac{k-1}{2}}</math></p>
14	<p>For <math>n \geq 3, \sum_{k=1}^n \mu(k!) =</math></p> <p>(a) 0                      (b) -1                      (c) 1                      (d) None of these</p>

15	$\sigma(145)$ is (a) 120      (b) 130      (c) 140      (d) 145
16	$\mu(162) =$ -1      (b) 1      (c) 0      (d) none of these
17	$\sigma(n)$ is odd (a) $n=15$ (b) $n=11$ (c) $n=8$ (d) $n=21$
18	Which of the following are perfect numbers
19	If $2^k - 1$ is prime ( $k > 1$ ), then $n = 2^{k-1}(2^k - 1)$ is a (a) Perfect number (b) Pell's number (c) Fermat's prime (d) Mersenne Prime
20	If $2^k - 1$ is prime then (a) $k$ is even      (b) power of 2      (c) $k$ is prime      (d) $k$ is an odd prime